

MEMS

How to evaluate the resolution of an accelerometer

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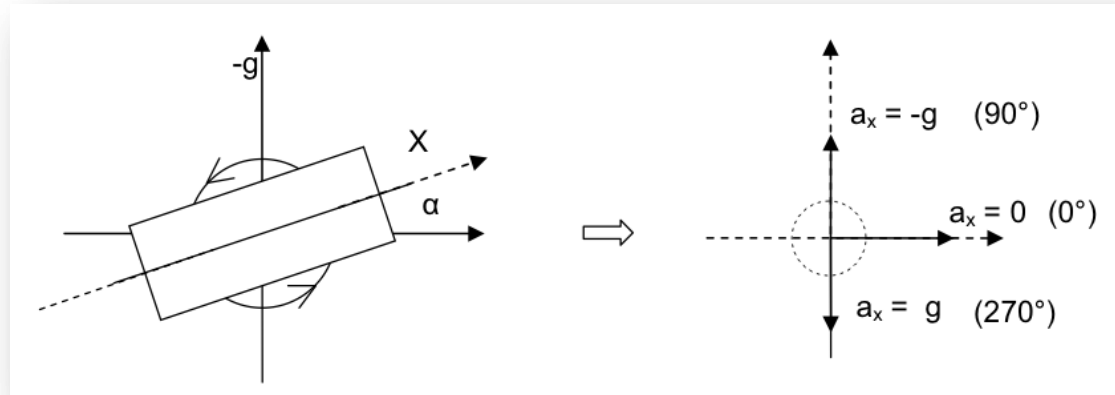
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Summary

- Ideal Inclinator: calculation of sensitivity $\text{mg} / ^\circ$ for an accelerometer (single axis, two-axis and three-axis)
- Real Inclinator: key parameters to be considered in order to evaluate sensitivity and accuracy in measuring the inclination

Single axis sensing



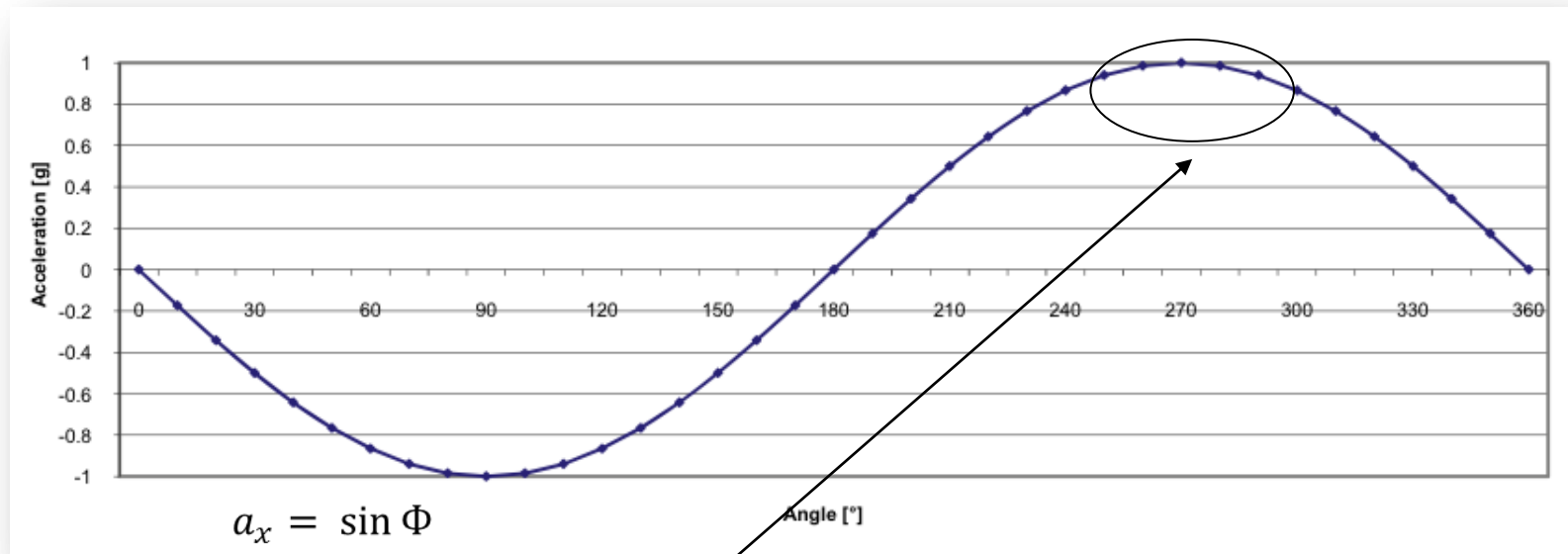
The X axis detects an acceleration equal to :

$$a_x = \sin \Phi$$

An accelerometer with sensing on a single axis does not allow to:

- Having a capacity of sensing constant to the variation of Φ : $a_x / ^\circ$ that depends on the function $\sin \Phi$
- does not distinguish between angles Φ and $(180 - \Phi)$

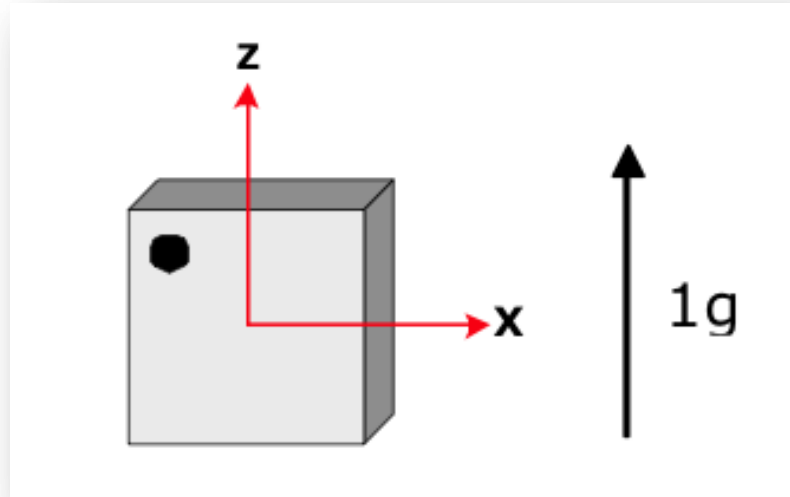
Single axis sensing



The sensor is less sensitive when its axis has a direction close to that of g

Φ	a_x [g]	$\Delta a_x / ^\circ$ [mg/°]
0	0.000	17.452
15	0.259	16.818
30	0.500	15.038
45	0.707	12.233
60	0.866	8.594
75	0.966	4.37
90	1.000	- 0.152

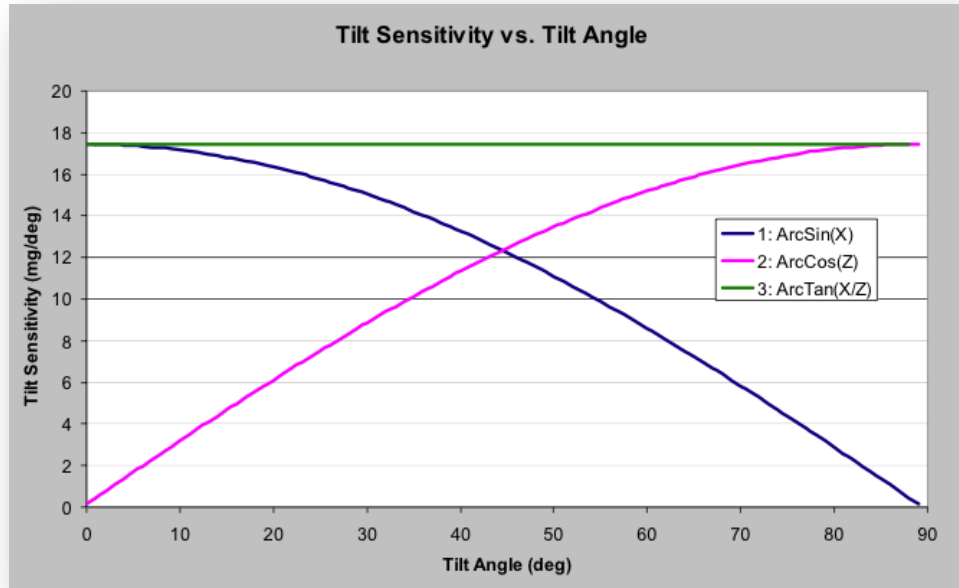
Two axes sensing



$$a_x = \sin \Phi$$
$$a_z = \cos \Phi$$

The use of two axes, one parallel and one perpendicular to $\vec{1g}$ allows to have a constant sensing Φ angle (on the plane x-z). This allows you to uniquely distinguish all the angle degrees.

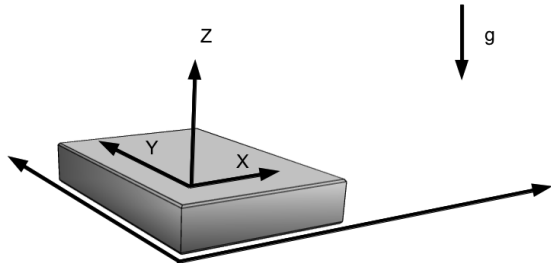
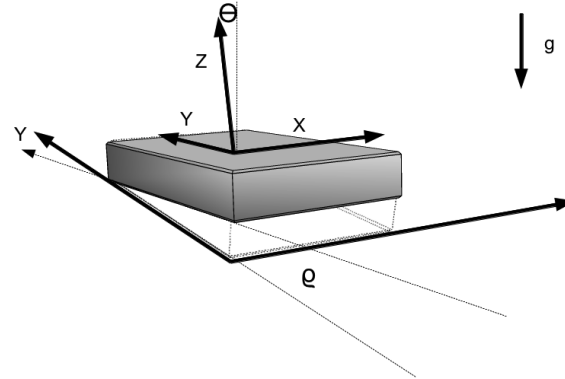
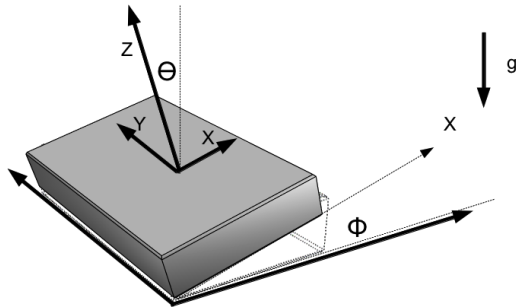
Two axes sensing



With the use of two axes x and z get a tilt sensing constant independent of the angle of rotation of approximately **17,45 mg / °**

Φ	a_x [g]	$\Delta a_x / ^\circ$ [mg/°]	a_z [g]	$\Delta a_z / ^\circ$ [mg/°]
0	0.000	17.452	1	-0.152
15	0.259	16.818	0.966	-4.664
30	0.500	15.038	0.866	-8.858
45	0.707	12.233	0.707	-12.448
60	0.866	8.594	0.500	-15.19
75	0.966	4.37	0.259	-16.897
90	1.000	0.152	0.000	-17.452

Three axis sensing



The reasoning can be extended on the axis
y - z:

$$\Phi = \arctan\left(\frac{Ax_1}{\sqrt{(Ay_1)^2 + (Az_1)^2}}\right)$$

$$\rho = \arctan\left(\frac{Ax_1}{\sqrt{(Ax_1)^2 + (Az_1)^2}}\right)$$

Accelerometer: key parameters

ODR (output data rate): typical value 100Hz

BW (bandwidth of the signal to be measured): typical ODR/2 or ODR/4

FS (full scale range): for example $\pm 2g$

SO (sensitivity): expressed in mg/LSB , indicates the variation of mg which must have to obtain a variation of one **LSB**

Resolution at: $1\sigma \Rightarrow A_n \cdot \sqrt{BW}$

The parameter 1σ corresponds statistically to (68.2% of samples), you should consider the value 3σ (99.7% of samples)

Accelerometer: key parameters

LIS331DLH: calculation resolution ($a \ 3\sigma$)

ODR = 50 Hz

BW = 25 Hz (ODR/2)

$$3 \cdot A_n \cdot \sqrt{BW} = 3,27 \text{ mg}$$

The accelerometer, taking into account the noise input, has a resolution of 3.27 mg.

Therefore, the resolution expressed in degrees will be:

$$\frac{3,27 \text{ mg}}{17,45 \text{ mg/}^\circ} = 0,187^\circ$$

Symbol	Parameter	Test conditions	Min.	Typ. ⁽²⁾	Max.	Unit
FS	Measurement range ⁽³⁾	FS bit set to 00		±2.0		g
		FS bit set to 01		±4.0		
		FS bit set to 11		±8.0		
So	Sensitivity	FS bit set to 00 12 bit representation	0.9	1	1.1	mg/digit
		FS bit set to 01 12 bit representation	1.8	2	2.2	
		FS bit set to 11 12 bit representation	3.5	3.9	4.3	
TCSO	Sensitivity change vs temperature	FS bit set to 00		±0.01		%/°C
TyOff	Typical zero-g level offset accuracy ^{(4),(5)}	FS bit set to 00		±20		mg
TCOff	Zero-g level change vs temperature	Max delta from 25 °C		±0.1		mg/°C
An	Acceleration noise density	FS bit set to 00		218		µg/√Hz
Vst	Self-test output change ^{(6),(7),(8)}	FS bit set to 00 X axis	120	300	550	LSb
		FS bit set to 00 Y axis	120	300	550	LSb
		FS bit set to 00 Z axis	140	350	750	LSb
Top	Operating temperature range		-40		+85	°C
Wh	Product weight			20		mgram